

Focus plus context visualization based on volume clipping for markerless on-patient medical data visualization

Márcio C. F. Macedo*, Antônio L. Apolinário Jr.

Department of Computer Science, Federal University of Bahia (UFBA), Brazil

Abstract

Focus plus context visualization can be used in augmented reality to improve the visual perception of the augmented scene. In the scope of in situ or on-patient medical data visualization, the focus plus context paradigm is used to improve depth perception for physicians showing the patient's anatomy as a focus region in the context of the patient's body. Volume clipping is one technique to realize focus plus context visualization. However, some of the existing methods for focus plus context visualization based on volume clipping do not run in full real time or are prone to artifacts. In this article, we present an extension for two of these techniques to improve performance and image quality of the original approaches. We validate all the techniques in a markerless augmented reality environment. A 3D reference model is tracked by the application, and volumetric medical data are shown to the user at the position of the patient's anatomy. Our technique is able to handle multiple anatomic regions, although the main region of interest used in this article is the face. Moreover, tracking accuracy is improved by the use of a hierarchical approach. From an evaluation of the proposed techniques, the results obtained highlight that all of them are free of artifacts, optimized for real-time performance, and improve the visual quality of the augmented scene.

Keywords:

Volume clipping, Focus plus context visualization, Augmented reality, Volume rendering

1. Introduction

Physicians see medical data, typically images of a patient's anatomic structures, on a monitor and they must analyze and mentally compose what is shown on the screen. This mental model of the patient's anatomy will help the physician provide health care in time-critical situations. Therefore, the physician must have sufficient knowledge of the patient's and general human anatomy to proceed appropriately during any medical procedure (e.g., diagnosis, surgery). With the availability of augmented reality (AR) technology, one can take over this task of mental mapping by transferring it to a computer. Therefore, the physician will be able to visualize, at the same time, the patient and a part of the patient's anatomy. On-patient or in situ medical data visualization can be used to improve surgical planning, training, medical diagnosis, and post-operative examination. This kind of application is desirable in fields such as those involving craniofacial data, in which the visualization of 3D examinations on the patient may help the physician understand the trauma.

AR is a technology which augments the view of a real scene with additional virtual information. Accurate tracking of the real scene, realistic rendering of the virtual data, and real-time user interactivity are the most important technical challenges of

AR applications [1]. The face is a part of the body in which depth- or texture-based tracking is easier because of the availability of face detection algorithms and the presence of distinguishable geometric structures. We take advantage of this to focus on the problem of on-patient medical data visualization for patients with craniofacial traumas. The decision to use a markerless AR (MAR) environment for tracking resulted from observations of the current limitations of the techniques proposed in the field of on-patient medical data visualization. Here, we are mainly interested in investigating the possibility of developing an MAR environment for on-patient medical data visualization which supports high-quality on-patient visualization and depth-based tracking (invariant to illumination conditions). Taking advantage of our main motivation to improve the physician's knowledge of the patient with craniofacial trauma, in this work we focused our tests on the patient's head as the region of interest (ROI). Although we have developed a solution for the scenario of craniofacial data visualization, in this article we show how the MAR environment can be adapted for other patient ROI (i.e., torso and pelvis; Section 6). The generality of the proposed work is discussed in this article.

Traditionally, on-patient medical data visualization applications superimpose virtual medical data on the patient. However, in such applications, the virtual content seems to be floating in front of the patient. As stated in previous work [2, 3, 4, 5], a better solution is to show the patient's anatomy as a focus region in the context of the patient's own body. This process is known as focus plus context (F+C) visualization paradigm [6],

*Corresponding author

Email addresses: marciocfmacedo@gmail.com (Márcio C. F. Macedo), apolinario@dcc.ufba.br (Antônio L. Apolinário Jr.)

52 and it is known to improve the visual perception of the con-
53 tent being visualized. In the field of volume rendering, one way
54 to improve the understanding and extend the exploration of the
55 medical volume is by use of volume clipping. Therefore, the
56 effect of volume clipping added in an F+C visualization tech-
57 nique is a new tool for the user to explore and understand the
58 augmented scene.

59 The existing techniques for F+C visualization based on vol-
60 ume clipping are prone to artifacts or do not run in full real
61 time [5]. Such issues decrease the application’s visual quality
62 and performance, respectively. One way to solve both problems
63 is by use of an adaptive strategy to mitigate artifacts and shaders
64 to execute the technique in parallel.

65 In this article, we present improvements in terms of perfor-
66 mance and visual quality over the F+C visualization techniques
67 based on volume clipping proposed in [5]. We expand the eval-
68 uation of the MAR environment for different ROI in the patient
69 and improve tracking accuracy through the use of a hierarchical
70 algorithm. A more detailed description of the algorithms used
71 in the entire solution (i.e., MAR environment and F+C visual-
72 ization) and an in-depth analysis of the results obtained and the
73 limitations of the proposed approach are presented as well.

74 The remainder of this article is organized as follows. Sec-
75 tion 2 reviews recent related work on medical AR and F+C
76 visualization applied in AR. Section 3 introduces the MAR en-
77 vironment used in this article for validation of the F+C tech-
78 niques. Section 4 presents the F+C techniques based on vol-
79 ume clipping for on-patient medical data visualization. Section
80 5 presents the tests conducted and the experimental results ob-
81 tained. Section 6 discusses the results obtained and the limita-
82 tions of this work. In Section 7, a summary of the article and
83 recommendations for future work are presented.

84 2. Related work

85 Medical AR systems for on-patient medical data visualiza-
86 tion have been driven by different approaches in recent years.
87 In this section, we classify the approaches on the basis of their
88 tracking technology: marker based or markerless.

89 Over the past decades, many relevant approaches have been
90 proposed for marker-based medical AR, such as those in [3, 4,
91 7]. Artificial fiducial markers provide fast and accurate tracking
92 because of their shape; however, they are commonly associated
93 with some issues which make this technology unsuitable for
94 on-patient medical data visualization applications:

- 95 • They are intrusive, because they are not part of the original
96 scene.
- 97 • When the traditional fiducial marker, such as the one used
98 in popular applications such as ARToolKit [8], is not used,
99 the optical tracking system hardware may be too expen-
100 sive.
- 101 • In general, this kind of tracking must operate only on the
102 image space, according to features computed from the pix-
103 els. The main drawbacks for this color- or texture-based

104 tracking are the susceptibility to illumination conditions
105 and marker occlusion, which may affect the accuracy of
106 the tracking algorithm.

107 Recently, systems have been proposed in the field of marker-
108 less medical AR. Some of them do not run in real-time (more
109 than 15 frames per second, FPS) [9, 10] and others rely on
110 specific prior knowledge about the ROI to be tracked (see
111 [11, 12, 13] for the body and [14] for the face). To the best of
112 our knowledge, there is only one exception which can be used
113 for general-purpose markerless on-patient medical data visual-
114 ization: the semiautomatic approach proposed in [15, 16, 17].

115 The semiautomatic MAR environment uses an RGB-D sen-
116 sor to reconstruct and track a 3D reference model of the pa-
117 tient’s ROI through the AR live stream. Then, after the virtual
118 medical data positioning, it can be displayed for a physician
119 at the location of the patient’s real anatomy. Real-time perfor-
120 mance is achieved by exploitation of the parallelism provided
121 by the graphics processing unit (GPU).

122 To validate the F+C visualization techniques, we use a
123 marker-free tracking algorithm because it requires a low pro-
124 cessing time and can operate on customer hardware with good
125 accuracy. A first necessary step is to evaluate the performance
126 and visual quality of the proposed approach. In this sense, the
127 semiautomatic MAR environment proposed in [15, 16, 17] is
128 used because it runs in real time and, with some adaptations, its
129 tracking solution can be applied for several ROI in the patient,
130 in contrast to other state-of-the-art solutions. Such adaptations
131 are discussed in Section 6.

132 An application for on-patient medical data visualization re-
133 quires special attention to be paid to the composition of the vir-
134 tual and real entities of the AR environment. Recently, many
135 approaches have been proposed in the field of F+C visual-
136 ization to dynamically define how this composition should be
137 done. These, also known as ghosting or X-ray vision tech-
138 niques, share the concept of an importance map, a mask (similar
139 to an alpha mask) which controls how real and virtual entities
140 should be blended.

141 Sandor et al. [18] designed a method for importance map
142 computation based on the feature regions of both real and vir-
143 tual objects inspired by three features: luminosity—to preserve
144 regions with high illumination; hue—to preserve strong colors;
145 motion—to preserve moving structures in the final rendering.
146 As stated by Sandor et al. [18], this work was an extension of
147 the work of [19], which is based on edge overlay to improve
148 spatial perception.

149 Mendez et al. [20] proposed an F+C technique in which
150 the lightness and color contrast of a given image are modified
151 according to the importance map computed from a live color
152 video. By adding subtle changes in the image, they guarantee
153 temporal and spatial coherence between frames. The problem
154 with this approach is its performance, which does not achieve
155 the full 30 FPS even when it is implemented on the GPU.

156 An adaptive F+C visualization technique was recently intro-
157 duced by Kalkofen et al. [21]. In their approach, an importance
158 map is computed for the occluder [20] and the occludee is in-
159 serted into the scene. Then, another importance map is com-

puted from this resulting image and is then compared against the first map computed. Regions on the first importance map that are not present in the final rendering are then emphasized to be visible. This approach improves the visual quality of the augmented scene and it runs in real time. However, it is not suitable for MAR environments, as it alone requires a processing time of 33 ms. Therefore, this additional time would decrease severely the performance of an MAR application.

F+C rendering was also proposed for visualization of underground structures in street scenes [22, 23, 24]. In these approaches, a method is used to dynamically compute when the underground structures must be rendered in relation to moving objects present in the scene. Although the final visual quality is good, the performance of the existing techniques is not full real time.

Traditional methods which compute the importance maps from live color video of the real scene are prone to errors because they are dependent on the illumination and material properties of the real environment. To overcome these problems, Mendez and Schmalstieg [25] proposed a method to compute an importance mask based on the 3D model of the scene. This task is accomplished by use of techniques such as mesh saliency [26] or through user interaction in a preprocessing step. The problem with this approach is that the importance mask creation requires some processing time. Therefore, the user cannot change interactively the importance mask during an AR live stream.

The methods proposed in the literature for F+C visualization in general AR applications capture the features of the image; however, their importance maps are not accurate enough to be used for medical applications.

F+C visualization has been proposed not only for AR, but also for volume rendering. In this case, it is used to define how the internal structures of the volume (e.g., bone, organ) should be visualized in the context of the soft tissue.

Bruckner et al. [27, 28] proposed a method for context-preserving volume rendering. From factors such as shading intensity, gradient magnitude, distance to the eye point, and previously accumulated opacity, the method allows the user definition of the F+C rendering according to only two parameters which controls these four factors to interactively change the transparency level between internal and external structures of the volume. The technique is easy to implement and runs directly on the shader. An extension of this algorithm was proposed by [29]. It incorporates rotation, scale, position, and mouse click to dynamically select focus and context regions.

Kruger et al. [30] proposed ClearView. Four layers (i.e., focus and context structures, isosurface's normal and curvature) are generated and composed for each frame in order to define the final visualization. The main disadvantages of this method is that it is naturally multi-pass (i.e., one shading pass is required to compute every layer) and the layers must be recomputed for every change of viewpoint. Therefore, the approach has a considerable cost in terms of performance.

Kirmizibayrak et al. [31] proposed a volumetric brush method for interactive definition of focus and context regions for volumetric models. Their approach runs in real time and

provides a good alternative for physicians to visualize medical data, especially for applications such as radiation therapy.

F+C solutions have also been proposed in the literature to help in the visualization of complex fiber distributions [32], blood flow [33], structured biomedical data [34] and ultrasound [35].

The main goal of the F+C visualization techniques applied in AR environments is to improve the depth perception of the augmented scene. This is specially important for medical AR applications, in which physicians must have good understanding of the augmented scene to proceed with their tasks appropriately. Despite the number of techniques and applications which have been proposed for medical AR, only a few of them consider the visualization a relevant aspect for the application [36]. We show here some of the visualization techniques proposed specifically for the field of medical AR to achieve the goal of improved depth perception.

Lerotic et al. [37] suggested the use of a pq space-based nonphotorealistic rendering method for augmented visualization in minimally invasive surgery. In their approach, the anatomic surface is expressed in terms of a pq -space representation, where p and q are the slope of the surface along the x and y axes. These values are used to determine which regions of the surface are more salient and must be emphasized in the final rendering. Pratt et al. [38] extended this technique to run in real time on the GPU. For it to do so, the original algorithm was simplified by use of an intensity gradient filter to highlight anatomic surface details.

Bichlmeier et al. [39] proposed the virtual mirror, a technique which improves not only the depth perception, but also the navigation, visualization, and understanding of the virtual structures positioned into the augmented scene. This can be achieved through the use of a specialized hardware setup and standard techniques in computer graphics for mirror reflection computation.

Kersten-Oertel et al. [40] provided an evaluation of several strategies for improving depth perception (namely, fog, pseudochromadepth, kinetic depth, edge depiction, and stereo) in the medical data visualization. The evaluation was conducted with novice and expert users, and the conclusion was that the fog and pseudochromadepth [41] techniques improve understanding of the medical structures.

One of the first techniques proposed for F+C visualization in the field of on-patient medical data visualization was the contextual anatomic mimesis (CAM) proposed by Bichlmeier et al. [2]. Its importance map is defined by three parameters: the curvature of the patient's skin surface, the angle of incidence (i.e., angle between the normal on the skin surface and a vector pointing from the position of the surface and the eye), and the distance falloff (i.e., the distance between each point on the surface and the intersection point of the line of sight and the skin surface). Differently from the color-based methods mentioned for the F+C techniques applied in the common AR scenario, this one operates directly on the shader and is not dependent on illumination or texture for the importance map definition. Although it provides improved visualization of the 3D medical data in the scene, it does not give special attention to the effect

274 of volume clipping.

275 Aiming to provide the physician with more tools to improve
276 the visual perception of the augmented scene, previous work
277 has proposed three F+C techniques based on volume clipping:
278 the smooth contours technique, and the visible background on
279 CT and MRI data techniques [5]. Each of them defines a spe-
280 cific region of the volume to be used as a focus or context re-
281 gion. However, the smooth contours technique is not optimized
282 for real-time performance, and the visible background on MRI
283 data technique generates images with visible artifacts and, in
284 fact, it was not evaluated with respect to visual quality, although
285 it showed promising results. In this article, we present an ex-
286 tension of the work of [5] to solve such problems.

287 3. Markerless augmented reality environment

288 In this section, we describe the MAR environment used in
289 this work, which is mostly based on the one proposed in [15,
290 16, 17]. However, we present modifications to improve tracking
291 accuracy while enabling real-time performance for the MAR
292 environment.

293 An overview of the proposed solution is given in Figure
294 1. First, we reconstruct a 3D reference model of the pa-
295 tient’s ROI to track it without markers in the AR live stream.
296 Three-dimensional (3D) reference model reconstruction re-
297 quires markerless tracking to align the different viewpoints ac-
298 quired from the patient’s ROI. In contrast, markerless track-
299 ing requires 3D reference model reconstruction to perform live
300 tracking during the on-patient medical data visualization. Be-
301 cause of the recent availability of MAR environments for on-
302 patient medical data visualization, which are based on off-the-
303 shelf hardware and provide good composition of the real and
304 virtual entities in the AR environment [17, 14, 13], they can
305 be used to validate the F+C techniques. From the estimated
306 camera pose (i.e., position and orientation), the medical vol-
307 ume can be rendered and displayed for a physician inside the
308 patient’s body at the location of the real anatomy. Volume
309 data are rendered according to standard volume rendering tech-
310 niques. After volume rendering, F+C visualization techniques
311 (i.e., smooth contours technique, and visible background on
312 CT and MRI data techniques) are used to define which parts
313 of the volume will be visualized in the final augmented scene.
314 Real-time performance is achieved by implementation of the
315 MAR environment (i.e., markerless tracking and 3D reference
316 model reconstruction) on the general-purpose GPU and vol-
317 ume rendering together with the F+C visualization using GLSL
318 shaders.

319 To track the medical volume in the AR environment without
320 markers, a 3D reference model of the patient’s ROI is generated.
321 To reconstruct a single 3D reference model of the patient’s ROI,
322 it is necessary to detect it and segment it from the real scene
323 captured by the RGB-D sensor. In this work, F+C visualization
324 techniques were validated in a scenario where the ROI consists
325 mainly of the patient’s face. For face detection and segmenta-
326 tion, the Viola-Jones face detector [42] is applied in the color
327 image provided by the RGB-D sensor. Once the ROI has been
328 segmented in the color image, this segmented region is fixed.

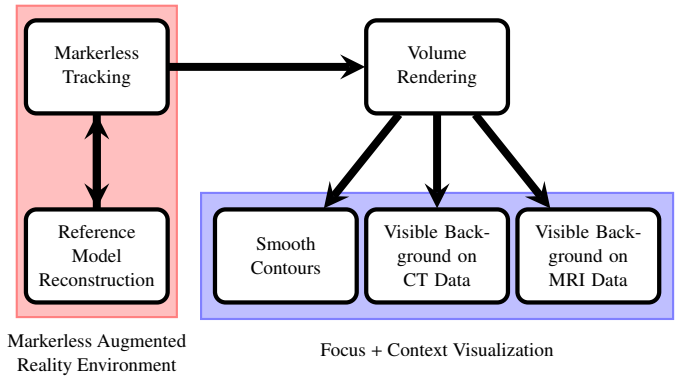


Figure 1: Integrated solution for markerless on-patient medical data visualization based on focus plus context rendering viewed as components and their relationships.

329 Then, the user is constrained to move the ROI in this fixed
330 region so that the system can capture the different viewpoints
331 from the same ROI. Through calibration of the color and depth
332 sensors, it is possible to transfer this segmented region of the
333 color image to the depth image. The depth map is denoised with
334 a bilateral filter [43], and then the pyramid algorithm is applied
335 to build low-resolution approximations of the original denoised
336 depth map [44, 45]. To do so, a mean filter is implemented on
337 the GPU to compute only two coarse levels from the denoised
338 depth map. Filtered depth maps are converted into vertex and
339 normal maps. Maps computed from the original depth map are
340 used through all the steps of the algorithm. Coarse vertex and
341 normal maps are used only for tracking. Then, the KinectFu-
342 sion algorithm [46] is used to reconstruct the reference model
343 of the patient’s ROI in real time.

344 KinectFusion is an algorithm that reconstructs high-quality
345 3D models from raw, noisy depth data captured from a depth
346 sensor. To do so, for each voxel a 3D grid stores the signed
347 distance to the closest surface and a weight that indicates the
348 uncertainty of the surface measurement. This volumetric rep-
349 resentation and integration is based on the VRIP algorithm
350 [47]. One extracts the implicit surface of this representation
351 (i.e., reference model) by detecting zero-crossings (i.e., posi-
352 tions at which the distance sign changes) on the grid through
353 a ray caster. This volumetric representation of KinectFusion is
354 especially useful for the F+C visualization based on the visible
355 background on MRI data technique, where the ray casting algo-
356 rithm is used to clip the 3D reference model directly from the
357 3D grid. Moreover, to keep the pyramid framework consistent,
358 a pyramid version of the ray cast data is built for each frame.

359 As evaluated in [48], the KinectFusion algorithm has max-
360 imum accuracy of approximately 10 mm; therefore, it is as-
361 sumed that its reconstructed models are suitable to be used as
362 reference for tracking and virtual data positioning in MAR ap-
363 plications which do not demand high accuracy. All of the steps
364 described above run in the GPU and are optimized for real-time
365 performance.

366 The 3D reference model is reconstructed only once, and it
367 is the basis for MAR live tracking. To position the medical

368 volume into the scene, a semiautomatic registration method is
369 used [17]. The virtual data are coarsely aligned with the 3D ref-
370 erence model (which represents the patient’s ROI data) in terms
371 of scale, positioning, and orientation. By controlling param-
372 eters such as the scale factor, rotation angles, and translation vec-
373 tor, the user is able to make fine adjustments (e.g., rescale the
374 virtual data, change the position of the virtual data, or modify
375 the orientation of the virtual data) over the coarse registration
376 in order to produce a more visually pleasant integration of the
377 medical data into the augmented scene.

378 After the placement of the medical data into the scene, the
379 markerless tracking is started. In fact, live tracking is done
380 in two steps: during the reconstruction of the 3D reference
381 model, to align the different viewpoints acquired from the pa-
382 tient’s ROI, and during the MAR with the patient and the med-
383 ical data. A real-time variant of the Iterative closest point (ICP)
384 algorithm [49] implemented on the GPU is used to estimate
385 the rigid transformation that aligns the current depth frame cap-
386 tured by the depth sensor with the previous one represented by
387 the 3D reference model. To improve tracking accuracy without
388 too much impact on performance, we use a hierarchical vari-
389 ant of the ICP algorithm, similarly as done in [50]. Hence,
390 we estimate the camera pose starting from the coarsest level to
391 the finest one using the previously computed vertex and normal
392 map pyramid. After each iteration, we update the final cam-
393 era pose estimated for the current frame. As discussed in the
394 Section 5, by controlling the number of iterations used for each
395 level of the tracking algorithm, we can trade off accuracy and
396 performance of the tracking in the MAR environment.

397 As stated in [46, 50], the use of the 3D reference model for
398 tracking allows a more consistent rigid registration with less in-
399 cremental error. However, in the presence of fast rigid motion
400 between frames, the ICP algorithm may fail (i.e., not converge
401 to a valid result). Taking advantage of the fact that the main
402 ROI in this article is a head, we used a real-time head pose esti-
403 mation [51] to provide a new initial guess to the ICP algorithm
404 to compute correctly the current transformation [52].

405 4. On-patient medical data visualization based on volume 406 clipping

407 4.1. Volume rendering

408 Volume rendering is a field concerned with techniques for
409 synthesizing images from 3D scalar data. This problem of im-
410 age synthesis is mathematically formulated as a volume render-
411 ing integral most commonly based on an emission-absorption
412 optical model [53].

413 To synthesize the medical image, a single rendering pass ray
414 casting is applied over the bounding box of the medical volume
415 [54]. To improve image quality and performance of the volume
416 rendering, several techniques are used as follows:

- 417 • Stochastic jittering (i.e., random ray-start)—to reduce
418 sampling artifacts;
- 419 • Fast GPU-Based tricubic filtering—to reduce filtering ar-
420 tifacts [55, 56];

- 421 • Empty-space leaping—to skip nonvisible voxels [57];
- 422 • Early ray termination—if the opacity accumulated is suf-
423 ficiently high;
- 424 • Preintegrated transfer functions—to capture high frequen-
425 cies introduced in the transfer functions defined with low
426 sampling rates [58];
- 427 • Blinn-Phong shading with on-the-fly gradient
428 computation—to add realism in the final rendering
429 [59];
- 430 • GPU tricubic prefilter—to improve tricubic filtering accu-
431 racy [60];
- 432 • Volume clipping—to extract and emphasize important
433 parts of the volume [53].

434 In this work, the volume is clipped according to six planes
435 parallel to the faces of the volume bounding box, although there
436 are several alternative techniques for volume clipping, such as
437 that in [61]. Nevertheless, we emphasize that the F+C tech-
438 niques can be used regardless of the technique used to crop the
439 volume.

440 After the volume rendering, medical data must be visualized
441 in the augmented scene. To achieve this goal, F+C visualization
442 is used to show the medical data in a focus region in the context
443 of the patient’s body, as described in the next subsection.

444 4.2. Focus and context visualization

445 We present improvements over the F+C visualization based
446 on volume clipping proposed in [5]. When one is clipping a
447 volume and rendering its image in an AR environment, there
448 will not be occlusion between the internal region of the volume
449 and the patient’s ROI, as shown in left image in Figure 2.

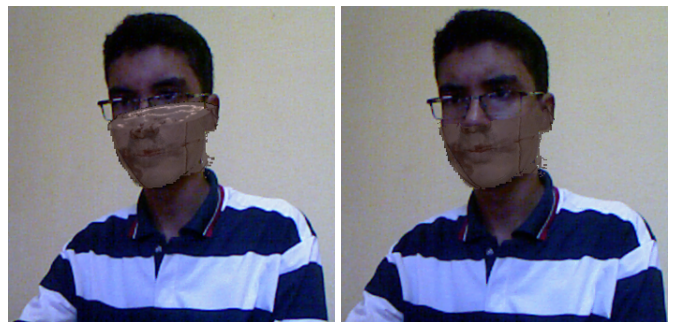


Figure 2: Occlusion between the volume’s internal structures and the patient’s region of interest. Left image: direct volume rendering with clipping. Right image: volume clipped rendered according to the proposed algorithm.

450 If desirable, one can solve this issue by changing the single-
451 pass ray casting [53]. We check if the first hit position of the
452 ray cast in the volume is in the clipped region. If it is, the ray
453 stops its traversal and is discarded from rendering. Otherwise,
454 the ray continues its traversal in the volume as normally done
455 in the standard ray casting algorithm. The visual effect of this

456 algorithm can be seen in the right image in Figure 2, where
457 the internal structures of the volume were removed in the final
458 rendering.

459 4.2.1. Smooth contours

460 When a volume is clipped, to reveal hidden structures of the
461 medical data, and its image is rendered in an AR environment,
462 edges located at the intersection between the volume and the
463 clipping planes become visible. This visibility of the edges oc-
464 curs not only in this region, but also for the entire contour of the
465 volume rendered (Figure 3, left image).



Figure 3: Influence of the smooth contours technique in the final rendering. Left image: direct volume rendering with clipping. Right image: volume clipped rendered according to the proposed algorithm. Contours are localized between the yellow shapes.

466 According to the F+C technique presented in [2], one can
467 improve depth perception by smoothing the transition between
468 the volume in the focus region and the rest of the AR scene. On
469 the basis of this, Macedo and Apolinario [5] proposed a new
470 method for F+C visualization based on the smooth contours
471 technique, an algorithm that adds a smooth transition between
472 the volume rendered and the real scene based on the volume
473 contours.

474 The smooth contours technique proposed in [5] consists of
475 the following steps: from the medical volume image, which is
476 loaded from the GPU to the CPU, it is converted to grayscale,
477 binarized by use of the threshold computed from Otsu's method
478 [62], contours are extracted from the method proposed by
479 Suzuki [63] and are smoothed by use of a Gaussian blur (kernel
480 size 3×3 pixels). The resulting image is a mask ($\alpha_{smoothCont}$)
481 which weights the blending of the volume and the patient's
482 color images. Also, a factor w_c can be dynamically defined
483 by the user to adjust the level of smoothing of the contours, ex-
484 panding or compressing the area of operation of the algorithm
485 (Equation 1). It ranges from 0, where the contours are ren-
486 dered, to $+\infty$, where the contour area is expanded, contours are
487 smoothed, and then suppressed in the final rendering because to
488 the high level of smoothness required.

489 Instead of the technique running entirely on the CPU, we
490 propose an alternative method for the technique to run entirely
491 on the shader, improving performance and achieving the same

492 quality of the final rendering. To achieve this goal, the pipeline
493 is changed as follows (Figure 4, top part): the medical volume
494 image is binarized by use of a predefined threshold t_b , which op-
495 erates on the gray intensity of each pixel (empirically we have
496 found $t_b = 0.1$ a good threshold for such a task), and the binary
497 image is blurred by one iteration of a two-pass Gaussian blur
498 (kernel size 3×3 pixels). Instead of explicitly computing the
499 contours by using Suzuki's method, we just apply the Gaussian
500 blur directly over the binary image. In practice, we have not
501 found a perceptual difference between these two approaches.
502 Moreover, as discussed in Section 5, with our new algorithm
503 we improved the performance of the original approach, as we
504 remove the need to transfer data from the GPU to the CPU,
505 which is a time-consuming step. Furthermore, because of the
506 separability of the Gaussian functions, the use of a two-pass
507 approach to convolve the binary image reduces the processing
508 time required by the filter while maintaining the same visual
509 result.

510 As can be seen in Figure 3, the smooth contours technique
511 softens the transition between the medical volume image and
512 the real scene. Furthermore, this method can be easily inte-
513 grated with other existing solutions, such as the CAM technique
514 [2]. An example of the result of such integration can be seen in
515 Figure 5. In the top image in Figure 5, a circular mask is defined
516 over the window to select which parts of the medical volume
517 must be rendered into the augmented scene. With the CAM
518 method, there is no clear handling of the contours which result
519 from the clipping the volume. By using the smooth contours
520 technique (Figure 5, bottom image), we can solve this problem
521 by smoothing the contours inside the focus window.

522 Two methods for F+C visualization that take advantage of
523 the clipping effect and the concept of a visible background were
524 proposed. They take advantage of the type of scanning technol-
525 ogy (CT or MRI) to enable new ways for physicians to visualize
526 and explore the medical data on the patient.

527 4.2.2. Visible background on CT data

528 In volume rendering, CT data can be used to enable the vi-
529 sualization of internal structures of the patient such as bones.
530 By designing an appropriate transfer function, one can visual-
531 ize the bone apart from the soft tissue of the volume. On the
532 basis of the color values associated with the soft tissue, the vir-
533 tual background used for rendering can be seen. In this case, it
534 is desirable to replace this virtual background by the real one,
535 enhancing the visual perception of the scene. Moreover, by use
536 of this strategy, the visualization of the soft tissue is deempha-
537 sized in the final rendering, emphasizing rather the focus region
538 of the visualization, the bone structure. The F+C visualization
539 based on the visible background on CT data technique can be
540 applied to enable this kind of visualization. An overview of this
541 method can be seen in the middle part of Figure 4.

542 The background scene is captured and stored in memory.
543 Next, the image of the volume after clipping is binarized and
544 sent to the shader as a foreground subtraction mask $I_{subtraction}$.
545 This mask identifies the region where the background can be vi-
546 sualized on the basis of the gray intensity of the volume. Then,
547 a user-defined threshold $w_{grayLevel}$ operates on the gray level of

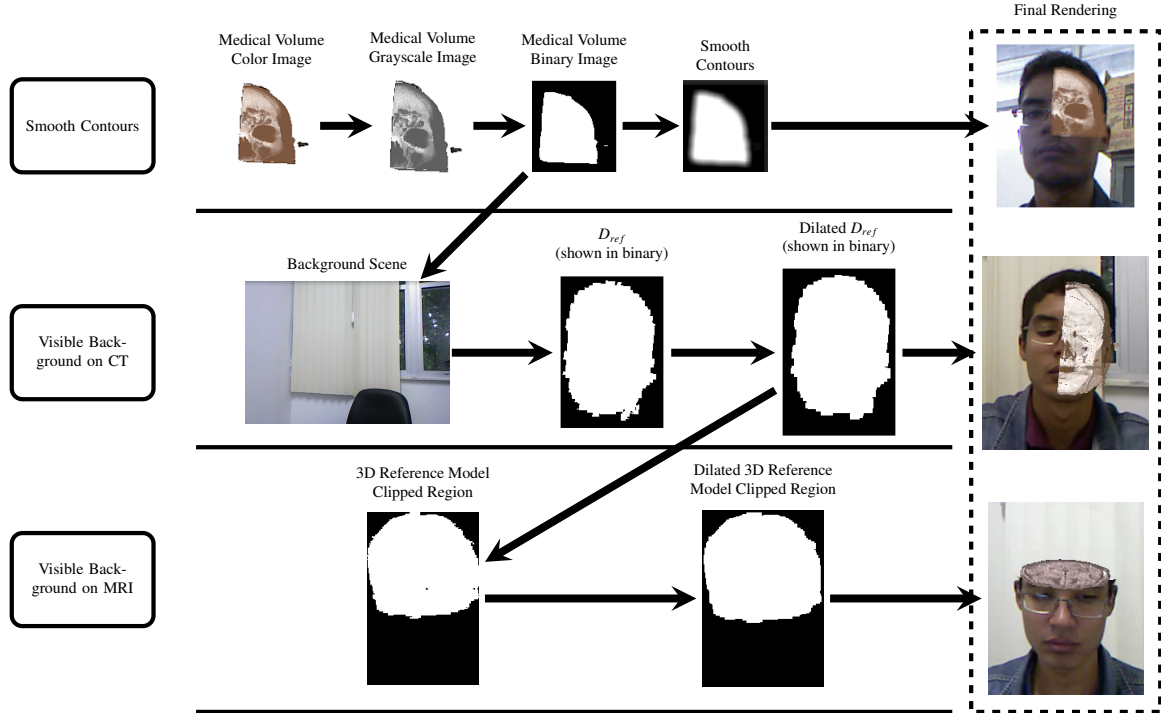


Figure 4: A schematic view of the proposed techniques. Focus plus context (F+C) visualization based on the smooth contours technique (top part): the blurred version of the binary image of the medical volume is used as a mask that smooths the transition between the medical data and the real scene on the final rendering. F+C visualization based on visible background on CT data technique (middle part): from the binary image of the medical volume, the dilated image of the 3D reference model, and the background scene, the soft tissue of the medical data can be displayed merged with the background, emphasizing the visualization of the bone structure. F+C visualization based on the visible background on MRI data technique (bottom part): by rendering a clipped image of the 3D reference model, the organs of the medical data can be displayed in the context of the patient’s region of interest.

548 the volume and separates bone and soft tissue regions, indicat-
 549 ing where the background scene must be rendered.

550 In our case, D_{ref} , the depth map of the 3D reference model,
 551 does not overlap perfectly with the patient’s ROI. To avoid the
 552 presence of artifacts in the final rendering, D_{ref} is dilated only
 553 on its contours to preserve the original depth (which is used for
 554 occlusion computation) and sent to the shader to represent the
 555 patient’s ROI.

556 4.2.3. Visible background on MRI data

557 In volume rendering, MRI data can be used to enable the
 558 visualization of internal structures of the patient’s anatomy such
 559 as organs. In an AR environment, the best way to visualize
 560 data of this kind is by clipping not only the medical volume but
 561 also the corresponding region of the patient’s color image. In
 562 this scenario, it is desirable to see the background scene in the
 563 region clipped, which is the main goal of the visible background
 564 on MRI data technique. An overview of this technique is given
 565 in the bottom part of Figure 4.

566 The technique originally proposed in [5] is similar to the one
 567 used for CT data. The background scene is saved. Next, tak-
 568 ing advantage of the volumetric representation of KinectFusion,
 569 which stores the 3D reference model as an implicit surface in
 570 a 3D grid, one can clip the patient’s ROI in real time. The
 571 algorithm to render an image from the 3D clipped reference
 572 model is given in **Algorithm 1**. This algorithm is an exten-
 573 sion of the pseudocode presented in [46]. We ray-cast the 3D

574 grid, and when the ray traverses a zero-crossing position (i.e.,
 575 the silhouette of the 3D reference model stored in the volume)
 576 and it is in the clipped region, the voxel’s corresponding pixel
 577 is rendered in the output image. The medical volume is clipped
 578 separately and sent to the shader. The output image from this
 579 algorithm is $I_{subtraction}$, which is used with the same objective
 580 as described for the visible background on CT data technique.
 581 Both $I_{subtraction}$ and D_{ref} are dilated because of the problem of
 582 overlapping described before.

583 The algorithm proposed in [5] is subject to the presence of
 584 artifacts at the intersection between the clipping plane and the
 585 3D reference model. To mitigate their effects, we use adap-
 586 tive sampling to reduce the step size of the ray when it is near
 587 the zero-crossing position. We check this proximity by using
 588 a specific threshold (t_{prox}) over the truncated signed distance
 589 function stored at the voxel g being traversed (g_{tsdf}). When
 590 near the zero-crossing, the step size of the ray cast is reduced to
 591 the value w_s to perform a more accurate traversal. From empir-
 592 ical tests, we have set $t_{prox} = 0.5$ and w_s equals to one fourth of
 593 the original step size. As shown in Section 5, by using this new
 594 algorithm, we improved the visual quality of the method while
 595 maintaining almost the same performance.

596 4.3. Final rendering

597 After the volume rendering, the color frame buffer is sent
 598 to the shader for blending with the patient’s color data coming
 599 from the RGB-D sensor. For the CAM and smooth contours

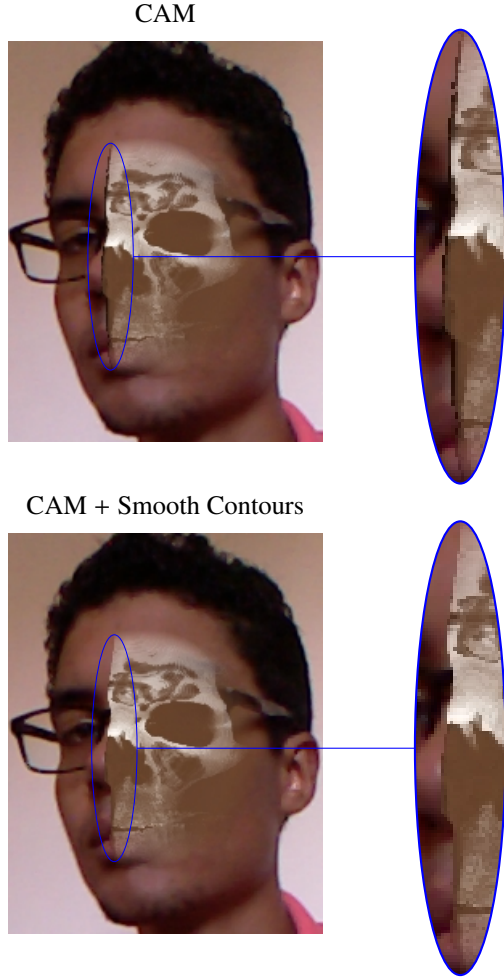


Figure 5: Focus plus context visualization based on the contextual anatomic mimesis (CAM) algorithm (top image) and its extension with the smooth contours technique (bottom image). By using the smooth contours technique, we can suppress the black border resulting from the clipping of the medical data, allowing a more seamless transition between real and virtual images.

600 techniques, blending is done by the following linear interpolation:
601

$$602 \quad I_{final} = \beta I_{real} + (1 - \beta) I_{medical} \quad (1)$$

603 where I_{real} is the image captured by the sensor, $I_{medical}$ is the
604 image corresponding to the medical volume, and I_{final} is the
605 resulting augmented image. In our approach, β is defined dyn-
606 amically, for every fragment/pixel, by the F+C visualization
607 techniques mentioned before, according to the following equa-
608 tion:

$$609 \quad \beta = clamp(max(w_c(1.0 - \alpha_{smoothCont}), \alpha_{CAM})) \quad (2)$$

610 where $clamp$ is a function that clamps the input parameter to
611 the interval $[0, 1]$.

612 For the visible background-based F+C techniques, the
613 shader listed in **Algorithm 2** is used instead of Equation 1, be-
614 cause this Equation does not include the background rendering.

Algorithm 1 Ray casting the clipped region of the 3D reference model volume

```

1: for each pixel  $\mathbf{u} \in$  output image  $I_{subtraction}$  in parallel do
2:    $I_{subtraction}(\mathbf{u}) \leftarrow 0$ ;
3:    $ray^{start} \leftarrow$  back project  $[\mathbf{u}, 0]$ ; convert to grid position
4:    $ray^{next} \leftarrow$  back project  $[\mathbf{u}, 1]$ ; convert to grid position
5:    $ray^{dir} \leftarrow$  normalize ( $ray^{next} - ray^{start}$ )
6:    $ray^{len} \leftarrow 0$ 
7:    $g \leftarrow$  first voxel along  $ray^{dir}$ 
8:   while voxel  $g$  within volume bounds do
9:      $ray^{len} \leftarrow ray^{len} + stepsize$ 
10:     $g^{prev} \leftarrow g$ 
11:     $g \leftarrow$  traverse next voxel along  $ray^{dir}$ 
12:    if  $g_{tsdf} < t_{prox}$  then
13:       $stepsize \leftarrow w_s$ 
14:    end if
15:    if zero crossing from  $g$  to  $g^{prev}$  and  $g$  is in the
      clipped region then
16:       $I_{subtraction}(\mathbf{u}) \leftarrow 255$ ;
17:    end if
18:  end while
19: end for

```

615 The algorithm for the visible background on CT data tech-
616 nique can be seen in lines 1-15 and 22-24. The color image
617 captured from the RGB-D sensor is rendered in the region that
618 does not represent the patient's ROI (i.e., where the depth of the
619 3D reference object is zero, as it was not reconstructed) (lines
620 2-4). The captured color image is also rendered when the vol-
621 ume is occluded and the occludee has depth (i.e., it is not in
622 a hole region) (lines 5-7). Next, if the fragment is in the sub-
623 traction mask region, the volume or the background scene is
624 rendered. Otherwise, the fragment is in the clipped region and
625 the real color image is rendered (lines 23-24). Gray intensity is
626 computed from the volume (by the $gray$ function) and assigned
627 to β . Considering that the bone is rendered with a gray level
628 greater than the soft tissue's and than $w_{grayLevel}$, it is rendered
629 without the background scene. Assuming that bone and soft
630 tissue have different gray intensities, $w_{grayLevel}$ can be adjusted
631 to render the bone with its original color and the soft tissue can
632 be linearly interpolated with the background scene (lines 8-15).

633 The algorithm for the visible background on MRI data tech-
634 nique is shown in lines 1-8 and 16-24. The color image cap-
635 tured from the RGB-D sensor is rendered in the same way as
636 described for the visible background on CT data technique. The
637 main difference here is that if the subtraction mask is active (i.e.,
638 the patient's ROI is clipped) and if there are medical data to be
639 visualized, they are rendered. Otherwise, the background im-
640 age is rendered.

641 In an AR environment, it is desirable to solve the problem
642 of occlusion between virtual and real data. For a specific view-
643 point, depth images of the patient's 3D reference model D_{ref}
644 and the 3D object coming from the sensor's live stream D_{live}
645 are used to solve this issue. If the depth from D_{live} is lower
646 than that from D_{ref} , the object captured by the sensor is in front
647 of the reference object and the medical volume is the occludee,

648 otherwise, the medical volume is the occluder.

Algorithm 2 Focus plus context visualization based on the visible background

```

1: for in parallel do
2:   if  $D_{ref} == 0.0$  then
3:     return  $I_{real}$ ;
4:   end if
5:   if  $D_{live} < D_{ref}$  and  $D_{live} \neq 0.0$  then
6:     return  $I_{real}$ ;
7:   end if
8:   if  $I_{subtraction} == 1.0$  then
9:     if CT data then
10:       $grayLevel \leftarrow gray(I_{medical})$ ;
11:       $\beta \leftarrow grayLevel$ ;
12:      if  $grayLevel < w_{grayLevel}$  then
13:        return  $\beta I_{background} + (1 - \beta)I_{medical}$ ;
14:      end if
15:      return  $I_{medical}$ ;
16:     else
17:       if  $I_{medical} == 0.0$  then
18:         return  $I_{background}$ ;
19:       end if
20:       return  $I_{medical}$ ;
21:     end if
22:   end if
23:   return  $I_{real}$ ;
24: end for

```

649 5. Experimental results

650 In this section, the performance and visual quality of the F+C
651 visualization techniques based on volume clipping are evalu-
652 ated.

653 5.1. Experimental setup

654 For all tests, as the computer we used an Intel Core™ i7-
655 3770K CPU (3.50 GHz), 8GB RAM, and a NVIDIA GeForce
656 GTX 660 graphics card. For 3D reference model reconstruction,
657 we used the open-source C++ implementation of Kinect-
658 Fusion released by the Point Cloud Library project [64].

659 We use a Microsoft Kinect device as a low-cost, accessible,
660 and versatile RGB-D sensor [65]. The medical dataset used
661 was a CT volumetric dataset of a head released by the Visible
662 Human Project [66] of resolution $128 \times 256 \times 256$, an MRI vol-
663 umetric dataset of a head from MRI Head available in Volume
664 Library [67] of resolution 256^3 , and an MRI dataset of a knee
665 of resolution $400 \times 400 \times 250$ and a CT dataset of a torso of res-
666 olution $512 \times 512 \times 288$, both available in OsiriX [68]. The 3D
667 reference models were reconstructed with KinectFusion with a
668 grid with resolution of 512^3 .

669 5.2. Performance evaluation

670 In our preprocessing computation, the 3D reference model
671 was reconstructed at 40 FPS. From empirical tests, the user

672 takes less than 10 s to place the volume into the scene and ad-
673 just it. The markerless live tracking and volume rendering tech-
674 niques together run at 45 FPS. These performance results are
675 the same as those reported in previous work [5]; however, they
676 were computed without taking into consideration the depth sensor's
677 performance¹.

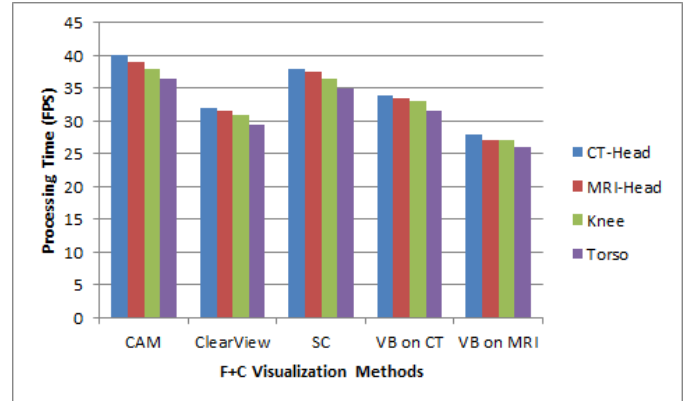


Figure 6: Performance results measured in frames per second (FPS) for each one of the focus plus context (F+C) visualization techniques discussed in this article. CAM, contextual anatomic mimesis; SC - smooth contours; VB - visible background.

678 The performance of the on-patient medical data visualization
679 for the F+C visualization techniques used in this work can be
680 seen in Figure 6. The performance was evaluated for all four
681 medical datasets described in Section 5.1.

682 From Figure 6, we see that the CAM technique provides the
683 best performance, which is expected since this technique does
684 small computations directly on the shader. For ClearView, an
685 F+C visualization technique proposed specifically for volume
686 rendering [30], we generated only one context layer and one
687 focus layer in our application. In the context layer, we com-
688 puted three layers (i.e., position, normal and curvature) for the
689 medical volume. For the focus layer, we rendered an isosurface
690 from the medical volume, according to a user-defined iso-value.
691 The layers were recalculated for every change in viewpoint. In
692 our application, ClearView requires approximately 6.25 ms to
693 compute and render these layers, which are composed accord-
694 ing to the distance-based importance shader [30], decreasing
695 the application's performance to a frame rate even lower than
696 that provided by the smooth contours and visible background
697 on CT data techniques. For the smooth contours technique, by
698 transferring all the pipeline to the GPU, we obtained a huge im-
699 provement over the original technique proposed in [5], which
700 achieved 20 FPS (for CT-Head in Figure 6) on the same hard-
701 ware. The visible background on CT data technique runs in full
702 real time because it operates mostly on the shader. Dilation ap-
703 plied on D_{ref} decreases the application's performance slightly.
704 The visible background on MRI data technique is slower than
705 the other techniques because of the ray casting performed on
706 the 3D reference model to render the clipped patient's ROI.

¹The Kinect sensor acquires depth data at 30 FPS; hence, this limits the maximum performance of the application.

707 However, differently from [5], we added an adaptive sampling
 708 scheme to improve the visual quality of the approach. This
 709 adaptive approach allowed us to obtain the same performance
 710 as the original technique. Moreover, all of the techniques run at
 711 more than 25 FPS, therefore in real time, even for the medical
 712 dataset of highest resolution (Torso in Figure 6).

713 5.3. Visual quality evaluation

714 By the use of the shader proposed in **Algorithm 2**, occlusion
 715 is supported by our application, as can be seen in Figure 7.



Figure 7: Occlusion support is achieved by comparing depth values from current and previous depth frames.

716 For the F+C visualization based on the smooth contours tech-
 717 nique, the level of smoothness can be controlled by the param-
 718 eter w_c . As can be seen in Figure 8, the transition between the
 719 volume and the real scene becomes smoother as w_c increases.
 720 At the same time, the volume contours become less visible.

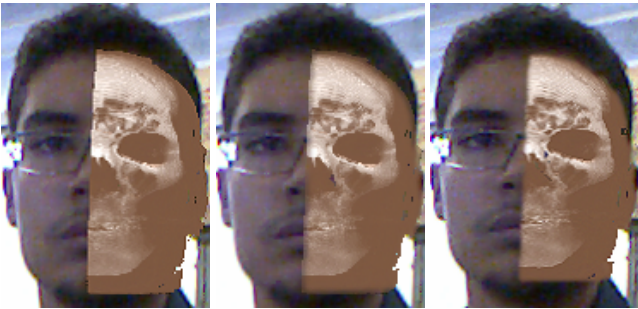


Figure 8: Influence of the parameter w_c in the smooth contours technique. Left image: $w_c = 0$. Middle image: $w_c = 2$. Right image: $w_c = 4$.

721 For the F+C visualization based on the visible background on
 722 CT data technique, bone and soft tissue structures can be separ-
 723 ated with use of $w_{grayLevel}$. From Figure 9, it can be seen that
 724 by changing this parameter, we can render the volume without
 725 the background scene, with the soft tissue linearly interpolated
 726 with the background scene or almost completely invisible.

727 For the F+C visualization based on the visible background on
 728 MRI data technique, we have proposed an improvement to miti-
 729 gate artifacts resulting from clipping of the patient's ROI [5]. A



Figure 9: Influence of $w_{grayLevel}$ in the visible background on CT data technique. Top-left image: $w_{grayLevel} = 0$. Top-right image $w_{grayLevel} = 0.5$. Bottom-left image: $w_{grayLevel} = 0.75$. Bottom-right image: $w_{grayLevel} = 1$.

730 visual comparison between our approach and the one proposed
 731 in [5] can be seen in Figure 10. As the artifacts become more
 732 visible during the user's movement, this figure shows the pa-
 733 tient's ROI in different positions and the presence of artifacts in
 734 these scenarios. Moreover, regions around the contours of the
 735 clipped data are zoomed to enable a clear visualization of the
 736 problems of related work [5] in comparison with the improve-
 737 ments proposed here. Artifacts at the intersection between the
 738 patient's ROI and the clipping plane are more visible when the
 739 user rotates his or her head in front of the sensor [5]. From col-
 740 umn I in Figure 10, we can see artifacts arising at the contours.
 741 By use of our approach (Figure 10, column II), artifacts are miti-
 742 gated and the results are comparable to a scenario (Figure 10,
 743 column III) where the ray is cast in a uniform sampling way and
 744 the step size of the ray is too small to render the clipped data
 745 in an AR application. In this case, our method has better per-
 746 formance than the best visual quality scenario, as ours runs at
 747 28 FPS, whereas because of its use of ray casting with a small
 748 step size, the ground-truth approach runs at only 9 FPS, which
 749 does not provide performance that is enough for an interactive
 750 application [69].

751 Our MAR environment supports not only rendering of the
 752 head, but also rendering of other ROI in the patient's body. The
 753 on-patient visualization of the torso and knee datasets with the
 754 CAM technique is shown in Figure 11, and can be found in the



Figure 10: Different schemes for focus plus context visualization based on the visible background on MRI Data technique. Column I results from the application of the original technique proposed in [5], column II refers to the adaptive scheme proposed in this article, and column III represents a ground-truth scenario where the ray casting performs uniform sampling and the step size of the ray is too small to render the clipped data in an interactive application. Our adaptive approach (column II) is three times faster than the ground-truth scenario (column III), while achieving almost the same visual quality. For each image, we zoom in on the contours of the clipped data to highlight the differences between the different approaches. Furthermore, red arrows are used to show regions where the visual difference is apparent. The presence of alias in the zoomed images is due to the digital zoom.

755 supplementary video. Even with different ROI, our MAR envi-
 756 ronment tracks the 3D reference model and shows the medical
 757 data at the position of the patient's anatomy. As the torso com-

758 prises mainly the abdomen and the pelvis, we have found it
 759 useful to show them separately.

760 The process to augment these structures over the patient's

body is almost the same as the one described in the previous sections. The small adaptations required to make the augmentation of other structures possible are discussed in Section 6.

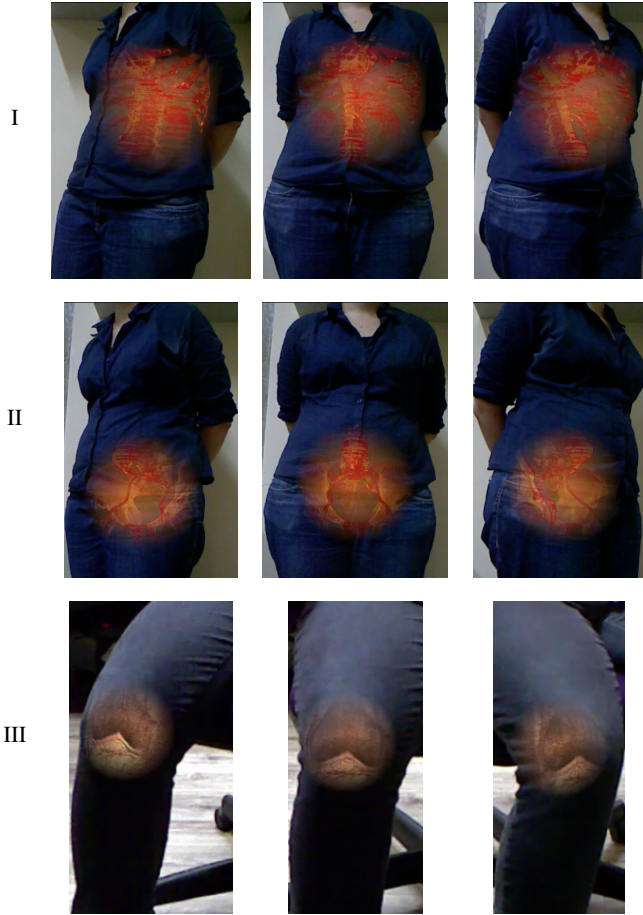


Figure 11: On-patient visualization of CT torso (rows I and II) and MRI knee (row III) datasets. To highlight the features of the CT torso dataset, we show the abdomen (row I) and pelvis (row II) separately.

Depending on the transfer function and/or the structure of the medical dataset, the ray casting technique may render holes in the final image (Figure 12, left image). In this case, the F+C techniques handle the holes in different ways, achieving different results for the final rendering. An example of this can be seen in the right image in Figure 12, where the smooth contours technique replaces the virtual background color of the hole by the color captured by the RGB-D sensor and smooths the contours around the hole region. The visible background on CT data technique replaces the virtual background color of the hole by the background color of the real scene, which was captured previously.

5.4. Accuracy evaluation

In all the experiments, the patient's ROI is augmented with a generic volumetric dataset. The use of a generic volume does not affect our visual quality evaluation since the volume is scaled and positioned semiautomatically with the user's fine adjustments [17]. In this way, the accuracy of the registration

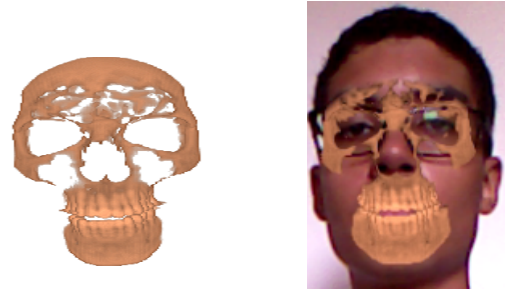


Figure 12: Medical volume with holes (left) rendered into the augmented scene with the smooth contours plus contextual anatomic mimesis (CAM) technique (right). For this figure, CAM's fall-off weight was set to 0.

between the medical data and the patient's ROI depends on the quality of the user's fine adjustment because of the use of a generic volume.

Related to the accuracy of the MAR environment, 3D reconstruction has accuracy of approximately 10 mm [48], and by using the hierarchical ICP algorithm, we improved the live tracking accuracy from approximately 3 mm [5] to approximately 2 mm, according to the point-to-plane error metric [49]. In this environment, tracking error does not accumulate between frames.

6. Discussion

As mentioned in Section 1, inspired by the field of on-patient craniofacial data visualization, we evaluated performance and visual quality of the proposed techniques in a scenario where the patient's ROI consists of the patient's head. In other contexts, where the ROI can be another part of the body, such as the abdomen, pelvis and knee (Figure 11), one can still use the solution presented in this article with minor adaptations. However, the MAR environment may still require some additional changes to reconstruct and track the poses. The main problems related to these adaptations rely on the segmentation, tracking and reconstruction of the patient's ROI.

To segment the patient's ROI in the scene, we propose the use of a classification algorithm to detect and segment it from the color image. This solution is desirable for a few ROI, such as the head and hand. For others, which do not have classification algorithms available to perform such a task, one solution is to position the ROI relatively distant from the background scene and segment it in the depth image with background segmentation through z-axis thresholding. For the scenarios shown in Figure 11, we used this strategy based on depth segmentation to remove the background scene.

Depth-based tracking algorithms (e.g., ICP) are dependent on the presence of geometric information on the scene [70]. Some ROI, such as the arm and leg, do not have much variation in the depth values captured by the sensor between different viewpoints. In this case, a texture-based tracking algorithm which operates according to the features of the color image [71, 72]

820 can be used to improve tracking accuracy. Furthermore, markerless tracking uses geometric data of part of the real scene as a natural marker. The natural marker (i.e., in our case the patient's ROI) may suffer nonrigid motion if it is a deformable object. For the patient's face or hand, for instance, it is desirable for the tracking algorithm to support non-rigid interaction between the patient and the application. Despite the complexity of nonrigid registration, there are some methods which provide real-time performance [73, 74] and can be used together with the markerless rigid tracking used in this work to improve accuracy and robustness for tracking of deformable structures. In all tests reported in this article, we used only the ICP algorithm for tracking.

833 For the hand and foot, ROI which contain smaller structures (e.g. fingers), more accurate 3D reconstruction algorithms [75, 73] may be required to reconstruct a 3D reference model which captures the finest details of the patient's ROI, hence enabling high-quality tracking and occlusion handling even in these smaller structures. In this situation, the KinectFusion algorithm is able to reconstruct acceptable 3D reference models for such ROI, although showing some artifacts which can have some impact on tracking accuracy. In this work, we used only the KinectFusion algorithm to reconstruct the 3D reference models.

844 As can be seen in the supplementary video, the use of a 3D reference model as a basis for markerless registration allows tracking of the medical data not only when the center of rotation is located at the position of the patient's anatomy. For knee visualization (Figure 11), the center of rotation is located mainly in the torso of the user, which is translated in relation to the knee region. Even in this case, our MAR environment supports the tracking of the medical data into the augmented scene.

853 By using the hierarchical tracking algorithm, we improved tracking accuracy, as mentioned in Section 5. The advantage of this improvement is twofold: for the reconstruction of the 3D reference model, in which the viewpoints captured by the depth sensor are rigidly aligned with more accuracy, resulting in a more accurate 3D reference model reconstruction; for the AR tracking, giving more tracking stability and less misalignment between real and virtual objects.

861 As already known in the field of AR, tracking technologies may suffer from jittering. As can be seen in the supplementary video, even when we used the hierarchical ICP algorithm together with the head pose estimation solution to improve tracking accuracy and robustness, the MAR environment is still prone to jittering when the user moves his or her ROI in front of the depth sensor. To minimize the jittering, one can increase the number of ICP iterations to trade off tracking accuracy and performance or change the tracking algorithm for another one which can explicitly handle such a problem. Hence, we empirically have found it useful to use only three iterations of the hierarchical ICP algorithm (i.e., one for each level of the pyramid), prioritizing performance over accuracy.

874 Markerless tracking solutions are not as accurate as some commercial marker-based solutions. When developing a medical AR application, one must decide carefully which of these

877 technologies to use. Although being intrusive in the scene, marker-based solutions may ease the positioning of the medical data into the scene and the tracking of the medical data with high accuracy, being recommended for medical applications that deal with surgery, as done in [2]. Markerless solutions are not very accurate, and are therefore recommended for applications which demand visually appealing results for the composition of real and virtual data, typically medical applications developed for training or visualization purposes [7].

886 For on-patient medical data visualization, the proposed application supports CT and MRI data, but can be easily extended to support other scanning data as well. Medical data with resolution higher than 512^3 can be used for a cadaver or phantom study. For such scenarios, the only difference is that the ROI is static in the scene and it is the sensor that must be moved to capture different viewpoints and reconstruct a single 3D reference model. We have evaluated the F+C techniques only for an in-vivo study with different users as a patient.

895 In AR applications, one must pay attention to the way in which the virtual content will be visualized in the augmented scene. In this article, we have described three techniques to improve the depth perception in medical AR scenarios. The artifacts present in the visible background on MRI data technique proposed in [5] decrease the quality of the final image in the region of the clipped medical data. This problem is even severer because of the high spatial and temporal discontinuity of the artifacts. Through the use of an adaptive scheme where the ray casting samples more voxels only at the location of the clipping plane, we achieved high-quality images (Figure 10, column II), almost indistinguishable from the ground-truth images shown in column III in Figure 10.

908 The techniques for F+C visualization based on the visible background do not support the visualization of real dynamic background scenes. In this case, we cannot use the color camera of the RGB-D sensor because the patient occludes part of the background being captured. A multiview approach, in which an additional webcam is used to capture the real background scene, may solve this problem.

915 7. Conclusion and future Work

916 We have presented improvements for on-patient medical data visualization by using F+C visualization and volume clipping. The performance and visual quality of the proposed techniques were evaluated, and from the tests conducted, we conclude that they are capable of running in real time and improve the visual quality of the final scene. To further enhance the quality of the integration of the virtual data into the augmented scene, occlusion is handled and tracking accuracy is improved. Finally, we have shown that our approach is versatile such that it can be used for different ROI of the patient.

926 In future work, we intend to evaluate the full solution (MAR environment and F+C techniques) in a real medical training environment, where high accuracy is not required for the application. Further, an in-depth study must be conducted to improve accuracy for scenarios where the medical dataset of the patient must be used for the on-patient visualization.

932 With feedback from specialists, we will be able to improve or
933 adapt the methods where needed or even to collect a database of
934 craniofacial data to further improve future tests and evaluations
935 of our approach.

936 For all the F+C visualization techniques proposed in this article,
937 quantitative evaluation and extensive user study must be
938 conducted to validate the proposed techniques from the perspective
939 of the final users.

940 For the AR environment, we used a conventional display to
941 show the augmented scene. Multiview solutions based on AR
942 glasses or portable solutions based on mobile devices can be
943 used, where the proposed approach is performed on a server
944 and the visualization of the augmented content is transferred to
945 those alternative hardware devices, allowing a seamless visualization
946 of the virtual content on the real scene.

947 The markerless tracking algorithm fails if the patient's ROI
948 is not visible in the view of the RGB-D sensor and the algorithm
949 does not support relocalization nor nonrigid registration
950 of the 3D reference model. These features must be supported
951 to further enhance the accuracy and robustness of the tracking.

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959 Amparo à Pesquisa do Estado da Bahia (FAPESB) and Coordenação
960 de Aperfeiçoamento de Pessoal de Nível Superior (CAPES).

962 [1] Azuma R, Baillot Y, Behringer R, Feiner S, Julier S, MacIntyre B.
963 Recent advances in augmented reality. *IEEE Comput Graph Appl*
964 2001;21(6):34–47. doi:10.1109/38.963459.

965 [2] Bichlmeier C, Wimmer F, Heining SM, Navab N. Contextual anatomic
966 mimesis hybrid in-situ visualization method for improving multi-sensory
967 depth perception in medical augmented reality. *ISMAR '07*; Washington,
968 DC, USA: IEEE. ISBN 978-1-4244-1749-0; 2007, p. 1–10.

969 [3] Kutter O, Aichert A, Bichlmeier C, Traub J, Heining SM, Ockert B,
970 et al. Real-time Volume Rendering for High Quality Visualization in
971 Augmented Reality. In: *AMI-ARCS 2008*. New York, USA: MICCAI
972 Society; 2008,.

973 [4] Wieczorek M, Aichert A, Kutter O, Bichlmeier C, Landes J, Heining SM,
974 et al. GPU-accelerated Rendering for Medical Augmented Reality in
975 Minimally-Invasive Procedures. In: *BVM 2010*. Springer; 2010,.

976 [5] Macedo MCdF, Apolinario AL. Improving on-patient medical
977 data visualization in a markerless augmented reality environment
978 by volume clipping. In: *Graphics, Patterns and Images (SIB-
979 GRAPI)*, 2014 27th SIBGRAPI Conference on. 2014, p. 149–56.
980 doi:10.1109/SIBGRAPI.2014.33.

981 [6] Card SK, Mackinlay JD, Shneiderman B, editors. *Readings in Information
982 Visualization: Using Vision to Think*. San Francisco, CA, USA:
983 Morgan Kaufmann Publishers Inc.; 1999. ISBN 1-55860-533-9.

984 [7] Debarba HG, Grandi J, Maciel A, Zanchet D. Anatomic hepatec-
985 tomy planning through mobile display visualization and interaction. In:
986 *MMVR*; vol. 173. IOS Press. ISBN 978-1-61499-022-2; 2012, p. 111–5.

987 [8] Kato H, Billinghurst M. Marker tracking and hmd calibration for a video-
988 based augmented reality conferencing system. In: *Augmented Reality,
989 1999. (IWAR '99) Proceedings*. 2nd IEEE and ACM International Work-
990 shop on. 1999, p. 85–94. doi:10.1109/IWAR.1999.803809.

991 [9] Maier-Hein L, Franz AM, Fangerau M, Schmidt M, Seitel A, Mersmann
992 S, et al. Towards mobile augmented reality for on-patient visualization

of medical images. In: *Bildverarbeitung für die Medizin. Informatik Ak-
tuell*; Springer. ISBN 978-3-540-19335-4; 2011, p. 389–93.

995 [10] Suenaga H, Hoang Tran H, Liao H, Masamune K, Dohi T, Hoshi K,
996 et al. Real-time in situ three-dimensional integral videography and surgi-
997 cal navigation using augmented reality: a pilot study. *International Jour-
998 nal of Oral Science* 2013;(2):98–102.

999 [11] Blum T, Kleeberger V, Bichlmeier C, Navab N. miracle: Augmented
1000 reality in-situ visualization of human anatomy using a magic mirror. In:
1001 *VR, 2012 IEEE*. 2012, p. 169–70. doi:10.1109/VR.2012.6180909.

1002 [12] Meng M, Fallavollita P, Blum T, Eck U, Sandor C, Weidert S, et al. Kinect
1003 for interactive ar anatomy learning. In: *Mixed and Augmented Reality
1004 (ISMAR)*, 2013 IEEE International Symposium on. 2013, p. 277–8.
1005 doi:10.1109/ISMAR.2013.6671803.

1006 [13] Stefan P, Wucherer P, Oyamada Y, Ma M, Schoch A, Kanegae
1007 M, et al. An ar edutainment system supporting bone anatomy
1008 learning. In: *Virtual Reality (VR)*, 2014 IEEE. 2014, p. 113–4.
1009 doi:10.1109/VR.2014.6802077.

1010 [14] Mercier-Ganady J, Lotte F, Loup-escande E, Marchal M, Lecuyer A. The
1011 mind-mirror: See your brain in action in your head using eeg and aug-
1012 mented reality. In: *Virtual Reality (VR)*, 2014 IEEE. 2014, p. 33–8.
1013 doi:10.1109/VR.2014.6802047.

1014 [15] Macedo MC, Apolinario AL, Souza AC, Giraldo GA. A semi-automatic
1015 markerless augmented reality approach for on-patient volumetric medical
1016 data visualization. In: *Virtual and Augmented Reality (SVR)*, 2014 XVI
1017 Symposium on. 2014, p. 63–70. doi:10.1109/SVR.2014.29.

1018 [16] Macedo M, Almeida C, Souza A, Silva J, Apolinario A, Giraldo G. A
1019 Markerless Augmented Reality Environment for Medical Data Visualiza-
1020 tion. In: *Workshop de Informatica Medica. WIM; Brazil; 2014,.*

1021 [17] Macedo M, Apolinario A, Souza AC, Giraldo GA. High-Quality On-
1022 Patient Medical Data Visualization in a Markerless Augmented Reality
1023 Environment. *Journal on 3D Interactive Systems* 2014;5:41–52.

1024 [18] Sandor C, Cunningham A, Dey A, Mattila VV. An augmented reality x-
1025 ray system based on visual saliency. In: *ISMAR. IEEE Computer Society;*
1026 2010, p. 27–36. doi:10.1109/ISMAR.2010.5643547.

1027 [19] Avery B, Sandor C, Thomas B. Improving spatial perception for aug-
1028 mented reality x-ray vision. In: *Virtual Reality Conference, 2009. VR
1029 2009. IEEE*. 2009, p. 79–82. doi:10.1109/VR.2009.4811002.

1030 [20] Mendez E, Feiner S, Schmalstieg D. Focus and context in mixed re-
1031 ality by modulating first order salient features. *SG'10*; Berlin, Heidel-
1032 berg: Springer-Verlag. ISBN 3-642-13543-9, 978-3-642-13543-9; 2010,
1033 p. 232–43.

1034 [21] Kalkofen D, Veas E, Zollmann S, Steinberger M, Schmalstieg D. Adap-
1035 tive ghosted views for augmented reality. In: *Mixed and Aug-
1036 mented Reality (ISMAR)*, 2013 IEEE International Symposium on.
1037 Adelaide, SA, Australia: IEEE Computer Society; 2013, p. 1–9.
1038 doi:10.1109/ISMAR.2013.6671758.

1039 [22] Schall G, Mendez E, Kruijff E, Veas E, Junghanns S, Reitingner B, et al.
1040 Handheld augmented reality for underground infrastructure visualization.
1041 *Personal Ubiquitous Comput* 2009;13(4):281–91. doi:10.1007/s00779-
1042 008-0204-5.

1043 [23] Chen J, Granier X, Lin N, Peng Q. On-line visualization of underground
1044 structures using context features. In: *Proceedings of the 17th ACM Sym-
1045 posium on Virtual Reality Software and Technology. VRST '10*; New
1046 York, NY, USA: ACM. ISBN 978-1-4503-0441-2; 2010, p. 167–70.
1047 doi:10.1145/1889863.1889898.

1048 [24] Padilha A, Rolim C, Teichrieb V. The ghosting technique applied to aug-
1049 mented reality visualization. In: *Virtual and Augmented Reality (SVR),
1050 2013 XV Symposium on*. 2013, p. 159–66. doi:10.1109/SVR.2013.36.

1051 [25] Mendez E, Schmalstieg D. Importance masks for revealing occluded ob-
1052 jects in augmented reality. In: *Proceedings of the 16th ACM Symposium
1053 on Virtual Reality Software and Technology. VRST '09*; New York, NY,
1054 USA: ACM. ISBN 978-1-60558-869-8; 2009, p. 247–8.

1055 [26] Lee CH, Varshney A, Jacobs DW. Mesh saliency. *ACM Trans Graph*
1056 2005;24(3):659–66. doi:10.1145/1073204.1073244.

1057 [27] Bruckner S, Grimm S, Kanitsar A, Gröller ME. Illustrative context-
1058 preserving volume rendering. In: *Proceedings of the Seventh Joint Euro-
1059 graphics / IEEE VGTC Conference on Visualization. EUROVIS'05*; Aire-
1060 la-Ville, Switzerland, Switzerland: Eurographics Association. ISBN 3-
1061 905673-19-3; 2005, p. 69–76. doi:10.2312/VisSym/EuroVis05/069-076.

1062 [28] Bruckner S, Grimm S, Kanitsar A, Gröller M. Illustrative
1063 context-preserving exploration of volume data. *Visualization and*

- 1064 Computer Graphics, IEEE Transactions on 2006;12(6):1559–69. 1135
1065 doi:10.1109/TVCG.2006.96. 1136
- 1066 [29] Sikachev P, Rautek P, Bruckner S, Gröller ME. Dynamic focus+context 1137
1067 for volume rendering. In: Proceedings of Vision, Modeling and Visual- 1138
1068 ization 2010. University of Siegen, Siegen, Germany; 2010, p. 331–8. 1139
- 1069 [30] Kruger J, Schneider J, Westermann R. Clearview: An interac- 1140
1070 tive context preserving hotspot visualization technique. Visualiza- 1141
1071 tion and Computer Graphics, IEEE Transactions on 2006;12(5):941–8. 1142
1072 doi:10.1109/TVCG.2006.124. 1143
- 1073 [31] Kirmizibayrak C, Wakid M, Yim Y, Hristov D, Hahn JK. Interactive foc- 1144
1074 us + context medical data exploration and editing. Computer Animation 1145
1075 and Virtual Worlds 2014;25(2):129–41. doi:10.1002/cav.1538. 1146
- 1076 [32] Röttger D, Merhof D, Müller S. The BundleExplorer: A Foc- 1147
1077 us and Context Rendering Framework for Complex Fiber Distribu- 1148
1078 tions. In: Proceedings of the Eurographics Conference on Visual 1149
1079 Computing for Biology and Medicine. EG VCBM'12; 2012, p. 1–8. 1150
1080 doi:10.2312/VCBM/VCBM12/001-008. 1151
- 1081 [33] Gasteiger R, Neugebauer M, Beuing O, Preim B. The flowlens: A focus- 1152
1082 and-context visualization approach for exploration of blood flow in cere- 1153
1083 bral aneurysms. Visualization and Computer Graphics, IEEE Transac- 1154
1084 tions on 2011;17(12):2183–92. doi:10.1109/TVCG.2011.243. 1155
- 1085 [34] Abellan P, Puig A, Ayala D. Focus + context rendering of structured 1156
1086 biomedical data. In: VCBM'08. 2008, p. 109–16. 1157
- 1087 [35] Schulte zu Berge C, Baust M, Kapoor A, Navab N. Predicate- 1158
1088 based focus-and-context visualization for 3d ultrasound. Visualiza- 1159
1089 tion and Computer Graphics, IEEE Transactions on 2014;PP(99):1– 1160
1090 doi:10.1109/TVCG.2014.2346317. 1161
- 1091 [36] Kersten-Oertel M, Jannin P, Collins D. Dvv: A taxonomy for 1162
1092 mixed reality visualization in image guided surgery. Visualization 1163
1093 and Computer Graphics, IEEE Transactions on 2012;18(2):332–52. 1164
1094 doi:10.1109/TVCG.2011.50. 1165
- 1095 [37] Lerotic M, Chung AJ, Mylonas G, Yang GZ. Pq-space based 1166
1096 non-photorealistic rendering for augmented reality. In: Proceedings 1167
1097 of the 10th International Conference on Medical Image Computing 1168
1098 and Computer-assisted Intervention. MICCAI'07; Berlin, Heidelberg: 1169
1099 Springer-Verlag. ISBN 3-540-75758-9, 978-3-540-75758-0; 2007, p. 1170
1100 102–9. 1171
- 1101 [38] Pratt P, Mayer E, Vale J, Cohen D, Edwards E, Darzi A, et al. An 1172
1102 effective visualisation and registration system for image-guided robotic 1173
1103 partial nephrectomy. Journal of Robotic Surgery 2012;6(1):23–31. 1174
1104 doi:10.1007/s11701-011-0334-z. 1175
- 1105 [39] Bichlmeier C, Heining S, Feuerstein M, Navab N. The virtual 1176
1106 mirror: A new interaction paradigm for augmented reality environ- 1177
1107 ments. Medical Imaging, IEEE Transactions on 2009;28(9):1498–510. 1178
1108 doi:10.1109/TMI.2009.2018622. 1179
- 1109 [40] Kersten-Oertel M, Chen SS, Collins D. An evaluation of depth enhancing 1180
1110 perceptual cues for vascular volume visualization in neurosurgery. Visu- 1181
1111 alization and Computer Graphics, IEEE Transactions on 2014;20(3):391– 1182
1112 403. doi:10.1109/TVCG.2013.240. 1183
- 1113 [41] Steenblik RA. The chromostereoscopic process: A novel single 1184
1114 image stereoscopic process. vol. 0761. 1987, p. 27–34. URL: 1185
1115 <http://dx.doi.org/10.1117/12.940117>. doi:10.1117/12.940117. 1186
- 1116 [42] Viola P, Jones MJ. Robust real-time face detection. Int J Comput Vision 1187
1117 2004;57(2):137–54. doi:10.1023/B:VISI.0000013087.49260.fb. 1188
- 1118 [43] Tomasi C, Manduchi R. Bilateral filtering for gray and color images. In: 1189
1119 Computer Vision, 1998. Sixth International Conference on. 1998, p. 839 1190
1120 –46. doi:10.1109/ICCV.1998.710815. 1191
- 1121 [44] Burt PJ. Fast filter transform for image processing. Com- 1192
1122 puter Graphics and Image Processing 1981;16(1):20 – 51. 1193
1123 doi:[http://dx.doi.org/10.1016/0146-664X\(81\)90092-7](http://dx.doi.org/10.1016/0146-664X(81)90092-7). 1194
- 1124 [45] Adelson EH, Anderson CH, Bergen JR, Burt PJ, Ogden JM. Pyramid 1195
1125 methods in image processing. RCA Engineer 1984;29(6):33–41. 1196
- 1126 [46] Izadi S, Kim D, Hilliges O, Molyneaux D, Newcombe R, Kohli P, et al. 1197
1127 Kinectfusion: real-time 3d reconstruction and interaction using a moving 1198
1128 depth camera. In: Proceedings of the 24th Annual ACM Symposium on 1199
1129 User Interface Software and Technology. UIST '11; USA: ACM. ISBN 1200
1130 978-1-4503-0716-1; 2011, p. 559–68. doi:10.1145/2047196.2047270. 1201
- 1131 [47] Curless B, Levoy M. A volumetric method for building complex mod- 1202
1132 els from range images. In: Proceedings of the 23rd Annual Confer- 1203
1133 ence on Computer Graphics and Interactive Techniques. SIGGRAPH '96; 1204
1134 New York, NY, USA: ACM. ISBN 0-89791-746-4; 1996, p. 303–12. 1205
- doi:10.1145/237170.237269.
- [48] Meister S, Izadi S, Kohli P, Hämmerle M, Rother C, Kondermann D. 1206
When can we use Kinectfusion for ground truth acquisition? In: IROS. 1207
IEEE Computer Society; 2012.. 1208
- [49] Rusinkiewicz S, Levoy M. Efficient variants of the icp algorithm. In: 1209
Third International Conference on 3D Digital Imaging and Modeling 1210
(3DIM). 2001, p. 145–52. 1211
- [50] Newcombe RA, Izadi S, Hilliges O, Molyneaux D, Kim D, Davison AJ, 1212
et al. Kinectfusion: Real-time dense surface mapping and tracking. In: 1213
Mixed and Augmented Reality (ISMAR), 2011 10th IEEE International 1214
Symposium on. 2011, p. 127–36. doi:10.1109/ISMAR.2011.6092378. 1215
- [51] Fanelli G, Weise T, Gall J, Gool LV. Real time head pose estimation from 1216
consumer depth cameras. In: Proceedings of the 33rd International Con- 1217
ference on Pattern Recognition. DAGM'11; Berlin, Heidelberg: Springer- 1218
Verlag. ISBN 978-3-642-23122-3; 2011, p. 101–10. 1219
- [52] Macedo M, Apolinario A, Souza A. A robust real-time face tracking 1220
using head pose estimation for a markerless ar system. In: Virtual and 1221
Augmented Reality (SVR), 2013 XV Symposium on. 2013, p. 224–7. 1222
doi:10.1109/SVR.2013.12. 1223
- [53] Hadwiger M, Kniss JM, Rezk-salama C, Weiskopf D, Engel K. Real-time 1224
Volume Graphics. USA: A. K. Peters, Ltd.; 2006. ISBN 1568812663. 1225
- [54] Hadwiger M, Ljung P, Salama CR, Ropinski T. Advanced illumination 1226
techniques for gpu-based volume raycasting. SIGGRAPH '09; New York, 1227
NY, USA: ACM; 2009, p. 2:1–2:166. 1228
- [55] Sigg C, Hadwiger M. Fast third-order texture filtering. In: Pharr M, 1229
editor. GPU Gems 2. Addison-Wesley; 2005, p. 313–29. 1230
- [56] Ruijters D, ter Haar Romeny BM, Suetens P. Efficient gpu-based texture 1231
interpolation using uniform b-splines. J Graphics Tools 2008;13(4):61–9. 1232
- [57] Li W, Mueller K, Kaufman A. Empty space skipping and occlusion clip- 1233
ping for texture-based volume rendering. In: VIS 2003. IEEE Computer 1234
Society; 2003, p. 317–24. 1235
- [58] Engel K, Kraus M, Ertl T. High-quality pre-integrated volume rendering 1236
using hardware-accelerated pixel shading. HWWS '01; New York, NY, 1237
USA: ACM. ISBN 1-58113-407-X; 2001, p. 9–16. 1238
- [59] Blinn JF. Models of light reflection for computer synthesized pictures. 1239
SIGGRAPH '77; New York, NY, USA: ACM; 1977, p. 192–8. 1240
- [60] Ruijters D, Thévenaz P. Gpu prefilter for accurate cubic b-spline inter- 1241
polation. Comput J 2012;55(1):15–20. doi:10.1093/comjnl/bxq086. 1242
- [61] Wu ST, Yauri Vidalon J, Souza Loos W, Coan A. Query tools for interac- 1243
tive exploration of 3d neuroimages: Cropping, probe and lens. In: Graph- 1244
ics, Patterns and Images (SIBGRAPI), 2013 26th SIBGRAPI - Confer- 1245
ence on. 2013, p. 250–7. doi:10.1109/SIBGRAPI.2013.42. 1246
- [62] Otsu N. A Threshold Selection Method from Gray-level Histograms. 1247
SMC 1979;9(1):62–6. doi:10.1109/tsmc.1979.4310076. 1248
- [63] Suzuki S. Topological structural analysis of digitized binary 1249
images by border following. CVGIP 1985;30(1):32 – 46. 1250
doi:[http://dx.doi.org/10.1016/0734-189X\(85\)90016-7](http://dx.doi.org/10.1016/0734-189X(85)90016-7). 1251
- [64] Rusu R, Cousins S. 3d is here: Point cloud library (pcl). In: ICRA. IEEE 1252
Computer Society; 2011, p. 1 –4. doi:10.1109/ICRA.2011.5980567. 1253
- [65] Cruz L, Lucio D, Velho L. Kinect and rgbd images: Challenges and 1254
applications. In: Graphics, Patterns and Images Tutorials (SIBGRAPI-T), 1255
2012 25th SIBGRAPI Conference on. 2012, p. 36–49. 1256
doi:10.1109/SIBGRAPI-T.2012.13. 1257
- [66] Visible human data. <http://www.nlm.nih.gov/research/visible/>; 2014. Accessed 22 September 2014. 1258
- [67] Volume library. <http://www9.informatik.uni-erlangen.de/External/vollib/>; 2014. Accessed 22 September 2014. 1259
- [68] Osirix. <http://www.osirix-viewer.com/datasets/>; 2015. Accessed 26 May 2015. 1260
- [69] Akenine-Moller T, Moller T, Haines E. Real-Time Rendering. 2nd ed.; 1261
Natick, MA, USA: A. K. Peters, Ltd.; 2002. ISBN 1568811829. 1262
- [70] Peasley B, Birchfield S. Replacing projective data association with 1263
lucas-kanade for kinectfusion. In: Robotics and Automation (ICRA), 2013 1264
IEEE International Conference on. 2013, p. 638–45. 1265
doi:10.1109/ICRA.2013.6630640. 1266
- [71] Lucas BD, Kanade T. An iterative image registration technique with an 1267
application to stereo vision. In: Proceedings of the 7th International Joint 1268
Conference on Artificial Intelligence - Volume 2. IJCAI'81; San Fran- 1269
cisco, CA, USA: Morgan Kaufmann Publishers Inc.; 1981, p. 674–9. 1270
- [72] Horn BK, Schunck BG. Determining optical flow. Artificial Intel- 1271

- 1206 ligence 1981;17(1-3):185 – 203. doi:[http://dx.doi.org/10.1016/0004-3702\(81\)90024-2](http://dx.doi.org/10.1016/0004-3702(81)90024-2).
- 1207
- 1208 [73] Zollhöfer M, Nießner M, Izadi S, Rhemann C, Zach C, Fisher M, et al.
1209 Real-time non-rigid reconstruction using an rgb-d camera. *ACM Trans-*
1210 *actions on Graphics (TOG)* 2014;33(4).
- 1211 [74] Souza ACS, Macedo MCF, Apolinário Jr. AL. Multi-frame adaptive
1212 non-rigid registration for markerless augmented reality. In: *Proceed-*
1213 *ings of the 13th ACM SIGGRAPH International Conference on Virtual-*
1214 *Reality Continuum and Its Applications in Industry. VRCAI '14*; New
1215 York, NY, USA: ACM. ISBN 978-1-4503-3254-5; 2014, p. 7–16.
1216 doi:10.1145/2670473.2670486.
- 1217 [75] Nießner M, Zollhöfer M, Izadi S, Stamminger M. Real-time 3d recon-
1218 struction at scale using voxel hashing. *ACM Transactions on Graphics*
1219 *(TOG)* 2013;.